# Robust and Efficient Ridge-Based Palmprint Matching

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Abstract—During the past decade, many efforts have been made to use palmprint as a biometric modality. However, most of the existing palmprint recognition systems are based on encoding and matching creases which are not as reliable as ridges. This affects the use of palmprints in large scale person identification applications where the biometric modality needs to be distinctive as well as insensitive to changes in age and skin conditions. Recently, several ridge-based palmprint matching algorithms have been proposed to fill the gap. Major contributions of these systems include reliable orientation field estimation in presence of creases and use of multiple features in matching, while the matching algorithms adopted in these systems simply follow the matching algorithms for fingerprints. However, palmprints differ from fingerprints in several aspects: 1) palmprints are much larger and thus contain a large number of minutiae, 2) palms are more deformable than fingertips, and 3) the quality and discrimination power of different regions in palmprints vary significantly. As a result, these matchers are unable to appropriately handle the distortion and noise despite heavy computational cost. Motivated by the matching strategies of human palmprint experts, we developed a novel palmprint recognition system. The main contributions are as follows: 1) statistics of major features in palmprints are quantitatively studied; 2) a segment-based matching and fusion algorithm is proposed to deal with the skin distortion and the varying discrimination power of different palmprint regions; and 3) to reduce the computational complexity, an orientation field based registration algorithm is designed for registering the palmprints into the same coordinate system before matching and a cascade filter is built to reject the non-mated gallery palmprints in early stage. The proposed matcher is tested by matching 840 query palmprints against a gallery set of 13,736 palmprints. Experimental results show that the proposed matcher outperforms the existing matchers a lot both in matching accuracy and speed.

Index Terms—Palmprint, orientation field, density map, data fusion, distortion, matching, cascade filtering, generalized Hough transform, naive Bayes classifier.

## **1** INTRODUCTION

THE human palm consists of two main features: flexion creases and friction ridges [1]. Flexion creases are formed due to the folding of the palm. The three most salient flexion creases, termed as major creases or principal lines [1], divide the palm into three regions: thenar, hypothenar and interdigital (see Fig. 1). The palm also contains many minor creases which are not as permanent as the major creases [1]. Friction ridges are formed as a result of a buckling instability in the basal cell layer of the fetal epidermis [2]. And an imaging resolution of about 500 ppi is required to observe the ridge feature. The patterns formed by the friction ridges on the palm are both unique and persistent, making it useful as a biometric trait for person identification. Law enforcement agencies throughout the world have been routinely collecting palmprints together with fingerprints from criminals since the early twentieth century [3].

Existing research on palmprint recognition mainly concentrates on low-resolution palmprint images which can be acquired using cheap cameras [4], [5], [6], [7], [8], [9], [10], [11]. The images are usually captured in contactless manner, and the resolution is about at 100 ppi. At such low resolution, ridges cannot be observed and matching is mainly based on major and minor creases. In [12], [13], [14], [15], researchers tried to explicitly extract and match major creases. In [5], [16], [17], [18], crease information is encoded and compared in various forms



Fig. 1. Crease and ridge features in a palmprint.

such as Gabor phase.

However, major biometric modalities used in large scale person identification systems, such as forensic and border control systems, need to be both distinctive and insensitive to changes in age and skin condition. Thus palmprint recognition systems for these applications have to be based on ridge features, although creases may be used as supplementary features. In fact, 500 ppi is the standard resolution for capturing palmprints in forensic applications [19] and person identification based only on ridge features (such as minutiae) is accepted in courts of law [1].

The literature of ridge-based palmprint recognition is still very sparse until now. In [20], Jain and Feng proposed a minutiae-based palmprint recognition system achieving acceptable accuracy. In this system, a region growing algorithm was proposed to extract the ridge orientation in presence of creases and a novel minutia descriptor, MinutiaCode, was designed. In [21], a multi-feature based palmprint recognition system was proposed by Dai and Zhou, where multiple features, including minutia points, orientation field, density map and major creases are extracted and compared to achieve higher accuracy.

Despite the available techniques, there are still some problems remaining to be solved for large-scale applications. Some of the most important problems are:

- 1) Skin distortion. Unlike finger tip, the palm contains many joints and its size is much larger. As a result, distortion is quite common between different impressions of the same palm, and much more serious than the distortion of fingerprints. Fig. 2 shows an example of palmprints with distortion. Since the algorithms in [20], [21] used a global rigid transformation model, they are fragile to large distortion.
- Diversity of different palm regions. Different regions of palmprints have varying quality and distinctiveness. While the existing algorithms in [20], [21] treat the identifying information from the different regions of a palm equally, it is important to weight such information according to its quality and distinctiveness to have a reliable matching procedure.
- 3) Computational complexity. Because palmprints in operational palmprint databases are usually not positioned in a common coordinate system, minutiae matching algorithms have to try all possible rotation and translation or all possible correspondence of minutiae. Since palmprints contains much more minutiae than fingerprints, those matching algorithms which are basically adapted from fingerprint matching algorithms are very inefficient in matching palmprints. For example, a well known commercial matcher, VeriFinger [22], can perform more than 15,000 fingerprint matches per second, but only three palmprint matches per second. The matching algorithms in [20], [21] are also very slow.

The limitations of the existing palmprint matching algorithms in [20], [21] can be summarized as that these algorithms are basically adapted from fingerprint matching algorithms [23], [24]. To develop an accurate and efficient palmprint matching algorithm, the intrinsic characteristics of palmprints have to be utilized.

Motivated by the matching strategies of human palmprint experts [1], [25], such as registering palmprints using clues from orientation field and rejecting nonmated palmprints based on partial region, we developed



Fig. 2. A pair of mated palmprints with large distortion, as indicated by the corresponding triangles.

a novel palmprint matching system for 1:N matching. The main contributions include:

- A quantitative statistical study of various characteristics of palmprints is conducted to guide the design and parameter selection of the matching system.
- 2) To deal with the distortion and the varying discrimination power of different palmprint regions, a segment-based palmprint matching and fusion algorithm is proposed. The whole palmprint image is divided into small segments which are then separately matched to deal with distortion. The similarity between two palmprints is calculated by fusing the similarity scores of different segments using a Bayesian framework.
- 3) To reduce the computational complexity, an orientation field based registration algorithm is designed for registering palmprints of different positions and rotations into the same coordinate system before matching. Furthermore, a cascade filter is built to reject non-mated gallery palmprints in early stage by comparing just a small portion of the whole palmprint.

Experimental results of matching 840 query palmprints against a gallery set of 13,736 palmprints show that the proposed algorithm achieves large improvement in both matching accuracy and speed. In fullto-full palmprint matching experiments, a True Acceptance Rate (TAR) of 97.9% is obtained by the proposed algorithm when the False Acceptance Rate (FAR) is controlled at  $2 \times 10^{-7}$ . This TAR is 17% higher than that of the algorithm in [21] and 40% higher than that of the algorithm in [20]. In partial-to-full palmprint matching, the TAR is 91.9% at a FAR of  $3 \times 10^{-8}$ , 34%and 65% higher than the TARs of the algorithms in [21] and [20], respectively. Experimental results also show that the proposed algorithm can improve the palmprint matching speed by a factor of 132 compared with the algorithm in [21].

The rest of this paper is organized as follows: In Section 2, the statistics of palmprint characteristics is analyzed. Section 3 describes the proposed palmprint matching algorithm. In Section 4, the experimental re-



Fig. 3. Average palmprint region mask. The bright pixels correspond to the location that tends to be valid palmar region.

sults are presented and analyzed. Finally, we finish with conclusions in Section 5.

## 2 STATISTICAL ANALYSIS OF PALMPRINTS

While qualitative knowledge on palmprints is sufficient for human experts, in order to design an automatic system and optimize its parameters, we need a quantitative study of palmprint features. In this section, the statistical characteristics of different palmprint features, different palmprint regions as well as palmprint distortion are discussed.

#### 2.1 Statistical Analysis of Different Features

The goal of a statistical study of palmprint features is to identify good features for registration and matching. A criterion is that the features with high consistency among different palms and low consistency among different regions of the same palmprint are useful for registering palmprints into the same coordinate system, while the features with high diversity among different palms are more important for matching.

To conduct a quantitative analysis of the features in palmprints, including orientation field and density map, we utilized 200 palmprints from 200 different palms. And they are composed of the first impressions of 40 different palms in the training set of the THUPALMLAB (see Table 3 for the details of this database) and another 160 palmprints further gathered from 160 palms. The palmprints are manually transformed into the same coordinate system, and those from the right hands are mirrored to increase the number of samples.

## 2.1.1 Region Mask

Region mask M of a palmprint I is a binary image where 1 indicates valid palmar region. Region mask is estimated using the algorithm in [20]. As shown by the average palmprint region mask in Fig. 3, the central regions of about 50% palmprints are missing. This is very common in palmprints captured using contactbased techniques.

## 2.1.2 Orientation Field

Orientation field characterizes the ridge orientation at each location in the palmprint. To study its statistical characteristic, the palmprint is divided into nonoverlapped blocks of  $64 \times 64$  pixels, and ridge orientation is estimated at each block using the algorithm in [20]. Let  $\theta_i(x, y)$  denotes the orientation at (x, y) of the  $i^{th}$ palmprint. We map it to a complex number of unit magnitude  $z_i(x, y) = \cos(2\theta_i(x, y)) + j\sin(2\theta_i(x, y))$  for computational convenience. The mean of  $z_i$  at (x, y) is:

$$\bar{z}(x,y) = \frac{\sum_{i \in T} z_i(x,y) M_i(x,y)}{\sum_{i \in T} M_i(x,y)},$$
(1)

in which  $M_i(x, y)$  is the region mask at (x, y) of the  $i^{th}$  palmprint.

The average and the circular standard deviation values for the orientation field at (x, y) are calculated by [26]:

$$\begin{cases} \bar{\theta}(x,y) = \frac{1}{2}Arg(\bar{z}(x,y)), \\ \sigma_{\theta}(x,y) = \frac{1}{2}\sqrt{-2\ln\bar{z}(x,y)}. \end{cases}$$
(2)

The derived average and circular standard deviation images are shown in Fig. 4 (a) and (b). As shown in Fig. 4 (b), a large portion of the palmar region has low deviation, and the circular standard deviation is below 15° in about 67% palmar region. This indicates there is a general ridge flow often repeated in the majority of the palmprints. Some common patterns in the orientation field of palmprints have been defined by palmprint experts [25], as shown in Fig. 5. In the thenar region, ridge flow forms a semi-circular pattern around the thumb, which is termed as "half-moon". In the hypothenar region, the characteristic is that ridges flow down and out of the hand. Near the top of the hypothenar region, ridges funnel toward the center. The ridges at the top side of the funnel are usually much flatter than those at the lower side. The orientation field shows common pattern between different palms and has large variance in different regions of the same palmprint, making it a good feature for registering different palmprints.

#### 2.1.3 Density Map

Density map depicts the ridge density of different locations in the palmar region. Density map is estimated by the algorithm in [21]. The average and standard deviation images of density map are shown in Fig. 6 (a) and (b), which are calculated by:

$$\begin{cases} \bar{d}(x,y) = \frac{\sum_{i \in T} d_i(x,y) M_i(x,y)}{\sum_{i \in T} M_i(x,y)}, \\ \sigma_d(x,y) = \sqrt{\frac{\sum_{i \in T} [(d_i(x,y) - \bar{d}(x,y))^2 \cdot M_i(x,y)]}{\sum_{i \in T} M_i(x,y) - 1}}, \end{cases}$$
(3)

in which  $d_i(x, y)$  is the ridge distance (reciprocal of ridge density) estimated at the  $16 \times 16$  pixels block



Fig. 4. Statistical characteristics of orientation field: (a) and (b) are the mean and circular standard deviation for the orientation field respectively. Note that bright pixels in (b) correspond to the location where singular points tend to appear.



Fig. 5. Common ridge flow patterns in the average orientation field.

around (x, y) for the *i*<sup>th</sup> palmprint,  $\bar{d}(x, y)$  and  $\sigma_d(x, y)$  are the average and standard deviation values of the ridge distance at (x, y). As is shown in the statistical results, the average ridge distance scatters in the range of 8 pixels to 12.5 pixels, while the standard deviation values are higher than 1.3 pixels in almost all the palmar region, showing low consistency among different palms.



Fig. 6. Statistical characteristics of density map: (a) and (b) are the mean and standard deviation for the ridge distance respectively.

## 2.2 Discrimination Power of Palmprint Features and Regions

Since ridge patterns in different palmar regions have different characteristics, the discrimination power of different regions also varies. In order to study this problem, a statistical experiment is conducted using the 8 impressions of 40 different palms in the training set. All the palmprints are transformed into the same coordinate system manually. Next, the transformed palmprint images are divided into non-overlapped blocks of  $64 \times 64$ pixels to save computational cost. The discrimination power of the  $510 \times 510$  pixel local region centered at each block is studied. The size is chosen so that there are sufficient features within to align successfully. When matching two palmprints, each block's local region is separately matched to the corresponding block's local region if they are valid palmprint regions. A total of 1,120 genuine matches and 101,280 impostor matches are performed using the algorithm in [21].

With the similarity scores of genuine and impostor match pairs from all the segments, the discrimination power of different features at different segments can be reflected by the True Acceptance Rate (TAR) when the False Acceptance Rate (FAR) is set as  $10^{-4}$ , as shown in Fig. 7.

It can be seen from Fig. 7 that the discrimination power of different area varies significantly. The interdigital and the hypothenar regions show better discrimination power than the thenar region. This is because there are many creases in the thenar, which significantly affect the extraction of ridge based features. It is also shown that among the features of minutiae, orientation field and density map, density map achieves the highest accuracy in most of the regions. Density map outperforms minutiae and orientation field in about 85% and 91% palmar regions respectively in the experiment. Some researchers have tried to apply it to fingerprint recognition but did not get a good result [27]. But this experiment proved that it is indeed a discriminating feature for palmprint recognition.

## 2.3 Distortion

The human hand has 27 bones, including the carpals in the wrist, the metacarpal bones running along the palm, and the phalanx bones in the fingers [28]. Due to the multiple degrees of freedom of the skeleton beneath the palm, distortion is very common in the palmar region. To study the distortion characteristic, a statistical experiment is conducted on the training set.

The registered palmprint images are divided into non-overlapped blocks of  $64 \times 64$  pixels as above. The distortion of the  $510 \times 510$  pixel local region centered at each block is studied. The 8 impressions of each palm are finely aligned with each other, generating 1,120 matching pairs in total. Each local region is aligned to the corresponding local region respectively using the generalized Hough transform based minutiae matching



Fig. 7. TARs of three different features at different palmprint regions when the FAR is set as  $10^{-4}$ : (a) minutiae; (b) orientation field; (c) density map.

algorithm [23], and the displacement parameters for all the local regions are recorded. For a given matching pair, let  $(\Delta x_k, \Delta y_k, \Delta \theta_k)$  denote the displacement parameters for the  $k^{th}$  local region, then the mean displacement between two palmprints is calculated by:

$$\begin{cases} \bar{\Delta x} = \frac{1}{N_a} \sum_{k=1}^{N_a} \Delta x_k, \\ \bar{\Delta y} = \frac{1}{N_a} \sum_{k=1}^{N_a} \Delta y_k, \\ \bar{\Delta \theta} = \frac{1}{2} atan(\sum_{k=1}^{N_a} \frac{\sin 2\Delta \theta_k}{\cos 2\Delta \theta_k}), \end{cases}$$
(4)

in which  $N_a$  is the number of corresponding local regions for the matching palmprint pair.

To characterize the distortion, the relative displacement  $(\tilde{\Delta}x_k, \tilde{\Delta}y_k, \tilde{\Delta}\theta_k)$  for each local region is calculated by subtracting the mean displacement from  $(\Delta x_k, \Delta y_k, \Delta \theta_k)$ . Finally, the average of the absolute values for the relative displacement parameters in each local region are calculated using all the matching pairs.

The calculated average absolute values are shown in Fig. 8. As shown in the image, distortion widely exists in the palmprint images, especially at the thenar region. The adduction/abduction movement of the human thumb is controlled by its carpal-metacarpal joint at the thenar region which is highly flexible [29], leading to greater susceptibility of the thenar regions towards distortion. And the distortion of other regions still cannot be ignored. Due to the universality of distortion in palmprints, distortion tolerant algorithms are required to achieve high accuracy for large-scale applications.

## 2.4 Summary

Major conclusions pertaining to palmprint characteristics are summarized as follows:

- Orientation field shows high consistency among the same region of different palms and low consistency among different regions of the same palmprint.
- Different regions and different features of the palmprint have varying discrimination power.
- 3) Distortion widely exists in the palmprint images.



Fig. 10. Relations between the three characteristics of palmprints and the three modules of the proposed matching algorithm.

## **3 PROPOSED PALMPRINT MATCHING SYSTEM**

## 3.1 System Outline

Motivated by the matching strategies of human palmprint experts and based on our quantitative study of palmprint statistics, we design a novel palmprint matching system for 1:N matching. The outline of the proposed palmprint matching system is shown in Fig. 9. The system is composed of three modules: palmprint registration, segment-based matching and fusion, and cascade filtering. The relations between the three modules and the major characteristics of palmprints summarized in Section 2.4 are shown in Fig. 10.

Since different palmprints share a lot of common ridge flow patterns, orientation field is used for palmprint registration, which transforms palmprints of different rotations and displacements into the common coordinate system. Thus, tight position constraint can be enforced in the matching algorithm, and matching speed can be greatly improved.

The segment-based matching and fusion algorithm is proposed to deal with distortion and varying discrimination power of different regions. Registered palmprints are divided into small segments. During palmprint matching, all the corresponding segments are finely aligned and compared respectively. When distortion occurs, the segments will rotate and shift to compensate for the distortion. In this way, the influence of distortion can



Fig. 8. Distortion characteristics of the palmprints: (a), (b) and (c) show the average absolute values of  $\Delta x_k$ ,  $\Delta y_k$ ,  $\Delta \theta_k$  respectively.  $\Delta x_k$  and  $\Delta y_k$  are in pixels, while  $\Delta \theta_k$  is in degrees.



Fig. 9. Outline of the proposed palmprint identification system.

be effectively reduced. The similarity score is calculated at each segment for each feature respectively, and the weights of various features at different segments are determined by learning.

As some segments in palmprints are very distinctive, it is possible to discard many non-mated gallery palmprints by just comparing these distinctive segments. The cascade filter is based on this idea.

In application, the proposed palmprint matching system operates as follows:

1) Palmprint registration is performed for the gallery palmprints in the enrollment stage and for the query palmprints in the identification stage separately. The gallery palmprints are generally full palmprints, while the query palmprints are live-scanned full palmprints from unknown suspects or latents recovered from crime scenes. The full palmprints are automatically registered by the proposed algorithm, while the latents are manually registered due to small palmar area, which is a common practice.<sup>1</sup>

- 2) Corresponding segments between the query and the gallery palmprints are compared sequentially based on an ordering determined by the cascade filter. Gallery palmprints which are very dissimilar to the query are rejected at once. Generally a large portion of the gallery palmprints are rejected after comparing just a few segments.
- 3) After cascade filtering, the query palmprint is matched with the remaining gallery palmprints by the segment-based matching and fusion algorithm to determine the true mate of the query palmprint.

## 3.2 Registration

Palmprint images in law enforcement databases are generally not in the same coordinate system since they are usually captured without posture and position restriction. Registration is thus necessary to bring different palmprints into the same coordinate system to facilitate the matching. Registration is an indispensable step in most biometric recognition techniques, such as iris [31], face [32]. Iris is generally registered by its inner and outer circular contours while face is generally registered by the location of eyes. The acceleration gained by registration is due to the tight position constraint in matching registered images. In case of minutiae matching, a minutia

<sup>1.</sup> The latents recovered from crime scenes are few and valuable. Palmprint experts usually manually mark the ridge features and determine the locations of latents based on the latent shape as well as some fine orientation field and crease features [25].



Fig. 11. Palmprint images captured by contactless techniques in laboratory environment (a) and by contactbased techniques in operational environment (b). The left one in (a) is from the CASIA palmprint database [16] and the right one in (a) is from the PolyU palmprint database [30].

point in the query palmprint just needs to be matched with a small portion of the minutia points in the gallery palmprint whose location and direction are similar to it, reducing the computational complexity significantly.

The key to registration is to find a good feature, which is similar between different palms, contains sufficient information to determine the correct position, and is robust to noise and incomplete impressions. Existing palmprint registration methods, which are based on intervals between fingers [4], [5], [33], [34], [35], hand contour [36] or principal lines [13], are mainly designed for contactless low-resolution palmprint verification systems. The low-resolution palmprints are captured by contactless devices, which ensures the whole palmar region and the finger roots are visible. However, in palmprints captured using contact-based techniques (such as inking and FTIR sensors, see Fig. 11), fingers are not available and principle lines and hand contours are usually incomplete or not reliable, making registration a challenging task. The statistical analysis in Section 2.1 shows that the orientation fields of different palms are quite similar and the orientation fields in different palmar regions are very distinctive, making orientation field a promising feature for palmprint registration.

Given the orientation field of an original (unregistered) palmprint, the registration algorithm first estimates the rigid transformation between the unregistered orientation field and the reference orientation field, and then registers the original palmprint with respect to the reference. The average orientation field shown in Fig. 4 is used as the reference orientation field for all the palmprints. And the unregistered orientation field



Fig. 13. Palmprints successfully registered by the proposed registration algorithm: (a) three original images from the same palm; (b) outputs of the registration algorithm.

is registered to both the reference orientation field (left palmprint) and the mirrored version (right palmprint). The unregistered palmprint is deemed left/right if it is more similar to the left/right reference. The algorithm in [20] is used to estimate orientation field on nonoverlapped large blocks ( $64 \times 64$  pixels) in order to suppress noise and reduce the computational complexity of the registration algorithm.

The orientation field of an unregistered palmprint can be viewed as a transformed and noisy version of the reference orientation field. The optimal rigid transformation between two orientation fields is found using the generalized Hough transform (GHT) algorithm [37]. All possible pairs of blocks between the unregistered and reference orientation fields are considered to vote for the corresponding transformation parameters: rotation, horizontal and vertical translation.

Since the features which are similar between different palms are important for registration, higher weights should be assigned to the votes from the regions with high orientation field consistence. Let w(x, y) denote the weight for the vote given by (x, y) in the coordinate of reference orientation field, it is calculated by:

$$w(x,y) = \frac{1}{1 + \sigma_{\theta}(x,y)},\tag{5}$$

in which  $\sigma_{\theta}(x, y)$  is the corresponding circular standard deviation of orientation field as defined in Equation (2).

After all pairs of blocks are considered, the bin in the transformation space with the largest number of votes is chosen as the transformation parameter.

The palmprint registration algorithm is used to speed up matching with as small accuracy reduction as possible. Therefore it is important to examine whether the different impressions of the same palmprint can be consistently transformed to the same coordinate system with



Fig. 12. Difference between the registration parameters estimated by the palmprint registration algorithm and the ground truth.

small deviation. We conducted a systematic experiment to automatically evaluate the consistence of registration for different impressions of the same palmprint. Eight impressions of the 40 different palms in the training set of THUPALMLAB are used in this experiment. The ground truth transformation parameters between palmprints are first estimated using the minutiae matcher in [21] and then manually verified. Fig. 12 shows the histograms of the difference between the registration parameters estimated by the proposed registration algorithm and the ground truth. The vast majority of the palmprints can be successfully registered with small difference. The example in Fig. 13 shows that although the three different impressions of the same palmprint are quite different in direction and impression region, the registration results are very consistent. According to the histograms of registration consistence in Fig. 12, the maximum rotation and displacement allowed in matching are set as  $20^{\circ}$  and five blocks of  $64 \times 64$  pixels respectively in our experiments.

#### 3.3 Segment-Based Matching and Fusion

As shown by the statistical results in Section 2, distortion usually occurs between palmprints, and the different features from different segments have large difference in discrimination power. Although some distortion models have been proposed for fingerprint [38], [39], [40], they are not suitable for palmprint because they are not efficient enough and the distortion of palmprints is much more serious. A segment-based matching and fusion algorithm is proposed to deal with the distortion and the varying discrimination power of different segments.

The registered palmprints are divided into  $4 \times 4$  nonoverlapped segments of  $510 \times 510$  pixels uniformly as in Fig. 9. The size is chosen so that there are sufficient features within each segment for successful minutiae matching, while the distortion within the segment is sufficiently small. Although there are numerous possible segmentation strategies, here we adopted this simple strategy to verify the effectiveness of our algorithm. The following procedures are performed at the segment level.

Each segment of  $510 \times 510$  pixels from the query palmprint is matched with the corresponding segment

from the gallery. Since the registration is coarse and may produce some deviations, the gallery segment is enlarged to  $610 \times 610$  pixels to completely contain the query segment. So the segments in the gallery palmprint are overlapped.

Before the matching is performed, first, the algorithm tests the completeness of the matching segments, which is measured by the foreground area size and the minimum minutiae number of the gallery and query segments within their overlapped palmprint region. In our algorithm, if the foreground area size is smaller than 76,800 pixels or the minimum minutiae number is less than 20, then the matching segments are deemed to be very incomplete and are not considered.

Next, the remaining matching segments are finely aligned by the generalized Hough transform based minutiae matching algorithm [41] with small tolerance. The maximum rotation and displacement allowed are set as 20° and five blocks of  $64 \times 64$  pixels respectively. After a segment is aligned, the number of matched minutiae within it is counted, and orientation field and density map are compared at blocks of  $16 \times 16$  pixels using the equations in [42] and [21]. The notation used in feature similarity calculation is summarized in Table 1, and the similarity scores are calculated as:

$$S_m = \frac{M}{M + M_E} \cdot \frac{M^2}{M_g M_q},\tag{6}$$

$$S_o = \frac{N_o}{N_o + N_{o_E}} \cdot (1 - D_o/90^\circ),$$
(7)

and

$$S_d = \frac{N_d}{N_d + N_{d_E}} \cdot \frac{1}{N_b} \sum_{i=1}^{N_b} \exp(-|d_g(i) - d_q(i)|), \quad (8)$$

in which  $M_E$ ,  $N_{o_E}$  and  $N_{d_E}$  are set as 5, 100 and 100, respectively.

After the above procedure, we get the similarity scores of three types of features for each segment. In addition, we observed that the consistence of the spatial transformations of segments can be used to distinguish genuine pairs from impostor ones, as shown in Fig. 14. The

TABLE 1 Notation in feature similarity calculation.

Notation	Meaning
$S_m$	Similarity score of minutiae
M	Number of matched minutiae.
$M_E$	Estimated minimal number of matched minutiae for the genuine.
$M_q$	Number of minutiae within the overlapped area for the query.
$M_g$	Number of minutiae within the overlapped area for the gallery.
$S_o$	Similarity score of orientation field.
$N_o$	Number of matched blocks where orientation field difference is within $22.5^{\circ}$ .
$N_{o_E}$	Estimated minimal number of blocks matched by orientation field for the genuine.
$D_o$	Mean of the orientation difference in all the blocks.
$S_d$	Similarity score of density map.
$N_d$	Number of matched blocks whose ridge distance difference is within 1 pixel.
$N_{d_E}$	Estimated minimal number of blocks matched by density map for the genuine.
$N_b$	Number of overlapped blocks between the match- ing segments.
$d_q(i)$	Ridge distance of the $i^{th}$ query block.
$d_g(i)$	Ridge distance of the $i^{th}$ gallery block.





Fig. 14. Spatial transformations of segments for genuine and imposter match pairs: (a) and (b) are two different impressions of the same palm, (c) is the spatial transformations of aligning (a) to (b); (d) and (e) are the impressions of two different palms, (f) is the spatial transformations of aligning (d) to (e).

relative displacement described in Section 2.3 depicts the consistence and is used as the feature.

Finally, the relative displacement, the similarity scores of minutiae, orientation field and density map are combined by Bayesian inference to output a match score. The probability that an observed palmprint match pair is genuine or impostor can be denoted by  $P(Y|\{(\tilde{\Delta}x_k, \tilde{\Delta}y_k,$ 

 $\hat{\Delta}\theta_k$ ,  $S_{m_k}$ ,  $S_{o_k}$ ,  $S_{d_k}$ )<sub> $k=1,\dots,16$ </sub>}), in which  $(\hat{\Delta}x_k, \hat{\Delta}y_k, \hat{\Delta}\theta_k)$  denote the relative displacement parameters for the  $k^{th}$  segment,  $S_{m_k}$ ,  $S_{o_k}$  and  $S_{d_k}$  are the segment's similarity scores of minutiae, orientation field and density map respectively, Y can take two values: G (Genuine) or I (Impostor). The dimension of the feature vector of the whole palmprint is 96. To avoid the curse of dimensionality, the features are supposed to be independent. The likelihood ratio of genuine versus impostor can be decomposed as:

$$L = \frac{P(G|\{(\Delta x_k, \Delta y_k, \Delta \theta_k, S_{m_k}, S_{o_k}, S_{d_k})_k\})}{P(I|\{(\tilde{\Delta} x_k, \tilde{\Delta} y_k, \tilde{\Delta} \theta_k, S_{m_k}, S_{o_k}, S_{d_k})_k\})}$$

$$= \frac{P(G)}{P(I)} \frac{P(\{(\tilde{\Delta} x_k, \tilde{\Delta} y_k, \tilde{\Delta} \theta_k, S_{m_k}, S_{o_k}, S_{d_k})_k\}|G)}{P(\{(\tilde{\Delta} x_k, \tilde{\Delta} y_k, \tilde{\Delta} \theta_k, S_{m_k}, S_{o_k}, S_{d_k})_k\}|I)}$$

$$= \frac{P(G)}{P(I)} \prod_{k=1}^{16} \frac{P((\tilde{\Delta} x_k, \tilde{\Delta} y_k, \tilde{\Delta} \theta_k, S_{m_k}, S_{o_k}, S_{d_k})|G)}{P((\tilde{\Delta} x_k, \tilde{\Delta} y_k, \tilde{\Delta} \theta_k, S_{m_k}, S_{o_k}, S_{d_k})|I)}$$

$$= \frac{P(G)}{P(I)} \prod_{k=1}^{16} \frac{P(\tilde{\Delta} x_k|G)P(\tilde{\Delta} y_k|G)P(\tilde{\Delta} \theta_k|G)}{P(\tilde{\Delta} x_k|I)P(\tilde{\Delta} y_k|I)P(\tilde{\Delta} \theta_k|I)}$$

$$= \frac{P(S_{m_k}|G)P(S_{o_k}|G)P(S_{d_k}|G)}{P(S_{m_k}|I)P(S_{o_k}|I)P(S_{d_k}|I)}$$

$$= \frac{P(G)}{P(I)} \prod_{k=1}^{16} L_k^s L_k^d, \qquad (9)$$

in which  $\frac{P(G)}{P(I)}$  is the prior likelihood ratio,  $L_k^s$  and  $L_k^d$  are the likelihood ratio values estimated according to the similarity scores and displacement parameters of the  $k^{th}$  segment respectively. And the likelihood ratio values for the incomplete segments are set as 1.

To avoid the influence of very poor quality segments on genuine matches, a regularization term is added. So the equation takes the form of:

$$L = \frac{P(G)}{P(I)} \prod_{k=1}^{16} (\epsilon + L_k^s L_k^d),$$
(10)

where the regularization term  $\epsilon$  is empirically set as 0.001.

In Equation (9), P(G)/P(I) is set as 1 and the PDFs are estimated using the results of matching the full palmprints from the training set. Gaussian Mixture Model (GMM) is used to approximate the 192 PDFs in Equation (9). The Expected Maximization (EM) algorithm [43] is performed to search for the best fit between the models and the observed samples.

#### 3.4 Cascade Filtering

Human experts can declare a pair of palmprints as unmatched as long as a portion of them is not matched [1]. The statistical result in Section 2.2 shows that some regions of the palmprint possess high discrimination power. Considering these facts, we develop a cascade filtering scheme to first compare these distinctive regions and quickly reject the dissimilar gallery palmprints. Cascade filtering is an important speedup technology in computer vision [44], [45], and multibiometrics [46]. Here we first describe how the cascade filtering works and then present how to construct the cascade filters.

A cascade filter containing M filters can be denoted by  $\mathbf{F} = \{(C_m, T_m)_{m=1,\dots,M}\}$ , in which  $C_m$  and  $T_m$  are the indices of the set of segments and the corresponding threshold used by the  $m^{th}$  filter, respectively. In cascade filtering, a pair of palmprints passes through the filters sequentially. At the  $m^{th}$  filter, the segments within  $C_m$ are matched, and the likelihood ratio is computed by:

$$L_{C_m} = \frac{P(G)}{P(I)} \prod_{k \in C_m} (\epsilon + L_k^s).$$
 (11)

The formula is different from Equation (10) in that just the likelihood ratio terms estimated by the similarity scores within the segments of  $C_m$  are used, since just the segments within  $C_m$  are available. If the calculated likelihood ratio,  $L_{C_m}$ , is lower than  $T_m$ , then the match pair is deemed as unmatched and quickly dropped. Otherwise, it is passed to the next filter and the above procedure repeats. In this way, most non-mated gallery palmprints can be rejected by just comparing a small region of the whole palmprint, resulting in a significant reduction of computational cost.

To construct a cascade filter, which segments to use in each filter should be determined, and appropriate thresholds should be chosen to exclude the non-mated palmprints while retaining the mated ones. Feature selection technique is brought in to determine the arrangements and parameters by viewing each segment as a feature. In most cases, the filter with more features can reject more non-mated pairs, while it takes more time to perform the filtering. To trade off between these two effects, our goal is to construct filters achieving desired True Rejection Rate (TRR) while keeping the False Rejection Rate (FRR) as 0 by using as few segments as possible. When building a filter, the possible combinations of segments form a search tree. The algorithm travels across this search tree in a breadth-first procedure. All possible filters using just one segment are first tested, and the best of them are selected. If the best one can reach the desired TRR, then the traversal procedure stops and the filter is built. Otherwise, all possible combinations of two segments are tested. The traversal procedure continues until the desired TRR cannot be achieved even using  $N_{max}$  segments. When a filter is built, it is added to the cascade filter. The segments used by the current filter are marked as occupied and the samples filtered are deleted. The algorithm tries to build the next filter with the left segments and training samples. So the cascade filter building procedure is a combination of greedy algorithm and exhaustive strategy. When building a specific filter, the exhaustive strategy is utilized. Once a filter is found, it will not change in the following search procedure, which is greedy.

The pseudocode of the algorithm for cascade filter construction is shown in Table 2. The inputs are the

TABLE 2 Pseudocode of the cascade filter construction algorithm.

**Function** ConstructCascadeFilter(L, Y) //Input: L – likelihood ratios of all the segments in the // training samples, Y – label array of the training samples //Output: F – constructed cascade filter do for number of segments to use, N, in 1 to  $N_{max}$  do generate combinations of N unoccupied segments  $\{C_{i_N}\}$ **foreach** combination  $C_{i_N}$  **do**  $[TRR_{i_N}, T_{i_N}]$ =ComputeTRRandThreshold( $C_{i_N}, L, Y$ ) end find the filter  $(C_{l_N}, T_{l_N})$  achieving the highest  $G_{l_N}$ if  $TRR_{l_N} > TRR_{desire}$  then add  $(C_{l_N}, T_{l_N})$  to the cascade filter mark the segments in  $C_{l_N}$  as occupied delete the samples filtered by  $(C_{l_N}, T_{l_N})$  from L, Ybreak end end while new filter is added output the constructed cascade filter  $\mathbf{F} = \{(C_m, T_m)_{m=1, \dots, M}\}$ 

likelihood ratios of all the segments in the training samples, L, and label array of the training samples, Y. In the algorithm of ComputeTRRandThreshold, the threshold,  $T_{i_N}$ , is set as the minimum likelihood ratio of the genuine match pairs and the corresponding TRR,  $TRR_{i_N}$ , is calculated.

## 4 EXPERIMENTS

#### 4.1 Palmprint Database

Till now, there is no publicly available high-resolution palmprint database to our knowledge. To test the algorithm, we collected 1,280 palmprint images from 80 subjects (two palms per person and eight impressions per palm) using a commercial palmprint scanner of Hisign. To increase the size of the gallery, 13,616 different palmprints (one impression per palm) provided by a local police department are used as the background database. All these palmprints images are of  $2040 \times 2040$  pixels and 500 ppi. The former set of 1,280 palmprints is termed as multi-impression subset and the latter is termed as uni-impression subset. As a whole, the database is termed as the THUPALMLAB, and it contains 320 more palmprints than the former database used in [21]. The multi-impression subset of THUPALMLAB is available at http://ivg.au.tsinghua.edu.cn. To simulate the latent prints recovered from crime scenes, we created partial palmprints from different regions of the full palmprints. For each palm in the multi-impression subset, 7 partial images are cropped from the thenar, hypothenar and interdigital regions of the last 7 impressions respectively. As a result, we obtain  $160 \times 21$  partial palmprints from 160 different palms. Since the partial palmprints are cropped to simulate the latents, they are manually registered as in real applications. In experiments, the prints from the first 40 palms of the multi-impression subset are used for training, while the left prints are used for testing. Among all the palmprint images, about 20% of

TABLE 3 Summary of the THUPALMLAB database.

Print type	Number of palmprints	Number of palms	
Multi-impression	Train	320	40
subset	Test	960	120
Uni-impression subset		13,616	13,616



Fig. 15. Two palmprints not successfully registered by the registration algorithm.

them are of relatively poor quality due to large amount of creases, deformation, smudges, blurs, incompleteness and etc. The database is summarized in Table 3.

#### 4.2 Performance of Each Module

In this subsection, we evaluate the performance of each of the three modules, i.e. registration, segment-based matching and fusion, and cascade filtering.

## 4.2.1 Registration

To test the speed up gained by registration, the GHTbased minutiae matching algorithm is used to match different impressions of the same palm. The average time for the fine alignment is counted on the whole THUPALMLAB. Without registration, we cannot make assumptions about the relative position between the matching palmprints. The maximum rotation allowed is 360° and the max displacement allowed is set as half of the palmprint image size. It takes about 5.1 seconds to match two full palmprints on average. When registration is performed, tight translation and rotation constraints can be applied. According to the histograms in Fig. 12, the maximum rotation and displacement allowed are set as  $20^{\circ}$  and five blocks of  $64 \times 64$  pixels respectively. The average time cost of matching two full palmprints using the same minutiae matcher is reduced to 78ms, which is about 65 times faster than without registration.

The computational cost of the registration procedure itself is composed of voting and best parameter searching, which are denoted by  $T_v$  and  $T_s$ .  $T_v$  is  $O(N_u \times N_r)$ and  $T_s$  is  $O(D \times D \times \Psi)$ , where  $N_u$  and  $N_r$  are the numbers of non-overlapped  $64 \times 64$  foreground blocks in the unregistered and reference palmprints respectively, D and  $\Psi$  are the maximum displacement and rotation allowed between the unregistered and reference palmprints. In experiments,  $T_v$  and  $T_s$  are about 900 for full palmprints, D and  $\Psi$  are set as half of the palmprint image size and 360° respectively. The execution time of the registration procedure is about 1.12s in our experiment. Since it is performed in the enrollment stage for the gallery palmprints and in the identification stage for the query palmprint only once, its computational cost takes a very small portion of the online identification procedure.

As for accuracy, 44 palmprints are not successfully registered, which is 0.3% of all the palmprints within the database. All the failure cases are due to improper impression or bad image quality. Two of the failed palmprints are shown in Fig. 15. Currently, we do not have an automatic method to determine whether the registration is correct or not. So these 44 palmprints also go through the cascade filtering and matching.

## 4.2.2 Segment-based matching and fusion

The segment-based matching and fusion algorithm comprises the advantages of being robust to skin distortion and making better use of varying discrimination of different palmprint regions. To verify the above advantages, we design three matching algorithms with different combinations of matching and scoring methods. In the first system, palmprints are aligned with global rigid transformations and feature similarity scores are calculated at global level as in [21]. The derived similarity scores are fused by a naive Bayesian with GMM. In the second system, palmprints are aligned at segment level, while feature similarity scores are still calculated globally and fused by a naive Bayesian. In the third system, palmprints are aligned and similarity scores are calculated at the segment level. The performance of these three matching algorithms in full-to-full and partial-tofull matching experiments are shown in Figs. 16. The experiment settings are the same as in Section 4.3.

It can be seen from Fig. 16 (a) that aligning at segment level can greatly improve the performance of matching full palmprints, for which distortion is a serious problem. The results of aligning the palmprints in Fig. 2 at global level and at segment level are shown in Fig. 17. It can be seen that aligning at segment level can effectively deal with the serious distortion. In partial-to-full matching, the system calculating and fusing similarity scores at segment level achieves higher accuracy than the system performs the operations at global level, as shown in Fig. 16 (b).

#### 4.2.3 Cascade filtering

The cascade filter is trained on the training set of THUPALMLAB. The maximum number of segments to use,  $N_{max}$ , and the desired TRR are set as 2 and 20%, respectively. The constructed cascade filter and its performance are shown in Fig. 18. The first filter uses the segment of C2, which corresponds to the region with



Fig. 17. Aligning the palmprints in Fig. 2 at different levels: (a) global level; (b) segment level.



Fig. 16. ROC curves of three matching and fusion methods: (a) matching 840 full palmprints against the gallery set of 13,736 palmprints; (b) matching 2,520 partial palmprints against the same gallery set.

outstanding discrimination power (see Fig. 7). By comparing one segment, this filter can reject up to 55.7% nonmated gallery palmprints while retaining all the mated gallery palmprints. The second filter uses the segment combination of B2 and D3, and 60.0% of the remained non-mated gallery palmprints can be rejected. But 1.1% of the mated gallery palmprints are also rejected. The third filter uses the segment combination of B3 and C3, resulting in a TRR of 22.4% and a FRR of 0%. As a whole, the constructed cascade filter achieves a TRR of 86.3% when the FRR is 1.1%. It can effectively reject the non-mated gallery palmprints by just comparing a small region of the palmprints.

The acceleration gained by cascade filtering is significant. Without cascade filtering, the segment-based matching and fusion algorithm takes about 151ms to match an impostor matching of full palmprints. When the cascade filtering is performed, the time is reduced to 39ms, resulting in an average acceleration rate of about 3.9.

In our experiment, when cascade filter is performed, the TAR of the proposed matching algorithm is about 97.9% when the FAR is set as  $2 \times 10^{-7}$ , which is 1.1% lower than the TAR of the algorithm without cascade filtering.

## 4.3 Overall Performance

The proposed matching algorithm was compared to the algorithms in [21] and [20] on the THUPALMLAB. The same feature extraction algorithm in [21] was used for all three matching algorithms. Both full-to-full palmprint matching and partial-to-full palmprint matching experiments were conducted. In these experiments, we



Fig. 18. Constructed cascade filter and its performance in filtering the matchings of 840 full palmprints against the gallery set of 13,736 palmprints.

used the full palmprints from 40 palms in the multiimpression subset as the training set to estimate the PDFs in Equation (9). The first impressions of the rest 120 palms in the multi-impression subset are combined with the uni-impression subset to form the gallery set of 13,736 palmprint images. The same galley set is used in both experiments. In the full palmprint matching experiment, the rest seven impressions of each of the 120 palms in the multi-impression subset are searched against the gallery set. In the partial palmprint matching experiment, the 21 partial impressions of each of the 120 palms are searched against the gallery set. When matching partial to full prints, the cascade filter is not used because the partial prints are very incomplete.

The performance is shown in both identification Receiver Operating Characteristic (ROC) curves [47] and verification ROC curves. Verification ROC curve is routinely reported for the convenience of comparison, while identification ROC curve measures the performance of the identification system. The identification system operates as follows. Given a query print, the system returns the gallery print whose similarity with the query is larger than the predefined threshold and is the largest one in all gallery prints. If there is no gallery print whose similarity is larger than the threshold, no gallery print is returned. An identification system may make two kinds of error: false negative identification and false positive identification. When the mate of the query is contained in the database but not returned by the system, a false negative identification occurs. When the database does not contain the mate of a query, but the system returns a gallery print, a false positive identification occurs. The false negative identification rate (FNIR) can be measured by performing a number of query whose mate is contained in the database and the false positive identification rate (FPIR) can be measured by performing a number of query which does not have a mate in the



Fig. 19. Identification ROC and verification ROC curves of the proposed algorithm, the algorithms in [21] and [20] in matching 840 full palmprints against the gallery set of 13,736 palmprints: (a) identification ROC curves; (b) verification ROC curves.

database. Since in our case, each query print has a mate in the database, the FPIR is obtained by setting the similarity with the mate as the lowest value. Another frequently used indicator, true positive identification rate (TPIR) is equal to 1-FNIR. By changing the similarity threshold, we can obtain a set of TPIRs and FPIRs and plot the identification ROC curve.

The identification and verification ROC curves of the full palmprint matching experiment are shown in Fig. 19. In the identification ROC curves, the TPIR of the proposed algorithm is about 97.9% when the FPIR is set as  $2 \times 10^{-3}$ , and it is about 17% and 43% higher than the algorithms in [21] and in [20] respectively. In the verification ROC curves, the TAR of the proposed algorithm is about 97.9% when the FAR is set at  $2 \times 10^{-7}$ , which is about 17% higher than the algorithm in [21] and 40% higher than the algorithm in [20].

The performance of partial-to-full palmprint matching systems are shown in Fig. 20. According to the identification ROC curves, a TPIR of about 91.9% is achieved by the proposed algorithm when the FPIR is



Fig. 20. Identification ROC and verification ROC curves of the proposed algorithm, the algorithms in [21] and [20] in matching 2,520 partial palmprints against the gallery set of 13,736 palmprints: (a) identification ROC curves; (b) verification ROC curves.

set as  $5 \times 10^{-4}$ , about 34% and 65% higher than the algorithms in [21] and [20] respectively. According to the verification ROC curves, the TAR of the proposed algorithm is 91.9% when the FAR is  $3 \times 10^{-8}$ , 34% and 65% higher than the TARs of the algorithms in [21] and in [20] respectively. The performance improvement for the partial-to-full matching system is more significant than that for the full palmprint matching system. That is because the influence of varying discrimination power of different palmprint regions is stronger for partial prints, as shown in Section 4.2.2.

To facilitate comparison with other algorithms, we also report the performance on the public multi-impression subset of THUPLAMLAB, containing 1,280 palmprints from 160 different palms. Since the first 40 palms have been used in the statistical study, the impressions from the left 120 palms are compared against each other in the testing stage. So 3,360 genuine matchings and 456,960 impostor matchings are generated to measure the performance. Since the gallery size (120) is very small, the performance of the proposed algorithm and the algorithms



Fig. 21. Verification ROC curves of the proposed algorithm and the algorithms in [21], [20] on the publicly available multi-impression subset of THUPALMLAB.

in [21], [20] are shown as the verification ROC curves in Fig. 21. Besides, we have made our algorithm publicly available on the web site of *http://ivg.au.tsinghua.edu.cn*, so that other researchers can test it on other palmprint datasets.

The computational costs of different algorithms are measured on a PC with Intel 2.4GHz CPU and Windows XP operating system. The feature extraction algorithm in [20] is used for all three matchers, which takes about 55s for processing a full palmprint. The matching time of different algorithms is shown in Table 4. The cascade filtering is not used for partial-to-full matching, so the speed of the proposed algorithm in partial-to-full matching is slower than that in the full-to-full matching. It should be noted that the proposed algorithm just uses a simple GHT-based minutiae matching algorithm to align palmprints, which is the same as in [21]. The experimental results show that the proposed algorithm improved the speed of the original matching algorithm in [21] by a factor of 132 for full-to-full impostor matching, which consumes most of the computational resources in large identification systems. Note that the acceleration is not only effective for GHT-based minutiae matching algorithm but also for other matching algorithms as well, including other minutiae-based methods [48], [49], [50], texture-based methods [24], [51], image-based methods [38] and so on.

## 5 CONCLUSION AND FUTURE WORK

In recent ten years, a number of palmprint recognition algorithms have been proposed and most of these algorithms are based on crease features extracted from low resolution contactless palmprints. However, creasebased palmprint recognition has not been successfully used for large scale person identification applications because of some inherent limitations. Ridge features in palmprints are proven unique and persistent and identification based ridge features is accepted in courts of law.

TABLE 4 Computational costs of different algorithms.

Algorithm	Full- matching	to-full time (ms)	Partial-to-full matching time (ms)	
	Genuine	Impostor	Genuine	Impostor
Proposed algorithm	161	39	62	57
Algorithm in [21]	5,364	5,158	2,763	2,678
Algorithm in [20]	2,019	1,906	657	623

Recently, a few ridge-based palmprint recognition systems have been proposed. Although there is some novelty in the feature extraction algorithms, the matching algorithms of these systems are basically adapted from fingerprint matching. Thus the accuracy of these systems is limited despite heavy computational cost. Motivated by the matching strategies of human palmprint experts, we quantitatively analyzed the statistics of palmprint characteristics and proposed a novel palmprint matching algorithm based on the obtained statistics, which achieves higher accuracy as well as lower computational cost than the previous systems. The main contributions include:

- 1) A quantitative statistical study on palmprints is conducted to guide the design of a robust and efficient 1:N palmprint matching system.
- 2) A segment-based palmprint matching and fusion algorithm is proposed to deal with distortion and varying discrimination power of different palmprint features and regions.
- An orientation field based registration algorithm and a cascade filter is designed to reduce the computational complexity in 1:N palmprint matching.

The proposed algorithm may also provide assistance for the low-resolution palmprint recognition [5]. The segment-based matching and fusion provides a strategy to deal with distortion and varying discrimination power of different regions for palmprint matching, while the cascade filtering idea may also be useful for acceleration.

The current registration algorithm is designed for registering full palmprints. But the palmprint experts can determine the location of a small latent palmprints based on certain clues, including the latent shape, some fine orientation field and crease features [25]. How to extend the current registration algorithm to partial and latent palmprints is an interesting but challenging problem. The registration algorithm needs to not only estimate the best spatial transformation but also output a confidence value associated with the transformation. Large law enforcement databases can contain as many as millions of palmprint images. While the current matcher is already significantly faster than existing matchers, its efficiency still requires large improvement.

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